

SIXTH EDITION

ESSENTIAL MATLAB[®]

for Engineers and Scientists

BRIAN H. HAHN
DANIEL T. VALENTINE

MATLAB
examples



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for Engineers and Scientists

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Academic Press is an imprint of Elsevier



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50 Hampshire Street, 5th Floor, Cambridge, MA 02139, United States
525 B Street, Suite 1800, San Diego, CA 92101-4495, United States
The Boulevard, Langford Lane, Kidlington, Oxford OX5 1GB, United Kingdom
125, London Wall, EC2Y, 5AS, United Kingdom

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Library of Congress Cataloging-in-Publication Data

A catalog record for this book is available from the Library of Congress.

British Library Cataloguing-in-Publication Data

A catalogue record for this book is available from the British Library.

ISBN: 978-0-08-100877-5

For information on all Academic Press publications
visit our website at <https://www.elsevierdirect.com>



Publisher: Todd Green

Acquisition Editor: Stephen Merken

Editorial Project Manager: Nate McFadden

Production Project Manager: Stalin Viswanathan

Designer: Matthew Limbert

Typeset by VTeX

Preface

The main reason for a sixth edition of *Essential MATLAB for Engineers and Scientists* is to keep up with MATLAB, now in its latest version (9.0 Version R2016a). Like the previous editions, this one presents MATLAB as a problem-solving tool for professionals in science and engineering, as well as students in those fields, who have no prior knowledge of computer programming.

In keeping with the late Brian D. Hahn's objectives in previous editions, the sixth edition adopts an informal, tutorial style for its "teach-yourself" approach, which invites readers to experiment with MATLAB as a way of discovering how it works. It assumes that readers have never used this tool in their technical problem solving.

MATLAB, which stands for "Matrix Laboratory," is based on the concept of the matrix. Because readers will be unfamiliar with matrices, ideas and constructs are developed gradually, as the context requires. The primary audience for *Essential MATLAB* is scientists and engineers, and for that reason certain examples require some first-year college math, particularly in Part II. However, these examples are self-contained and can be skipped without detracting from the development of readers' programming skills.

MATLAB can be used in two distinct modes. One, in keeping with the modern-age craving for instant gratification, offers immediate execution of statements (or groups of statements) in the Command Window. The other, for the more patient, offers conventional programming by means of script files. Both modes are put to good use here: The former encouraging cut and paste to take full advantage of Windows' interactive environment. The latter stressing programming principles and algorithm development through structure plans.

Although most of MATLAB's basic ("essential") features are covered, this book is neither an exhaustive nor a systematic reference. This would not be in keeping with its informal style. For example, constructs such as `for` and `if` are not always treated, initially, in their general form, as is common in many texts, but are gradually introduced in discussions where they fit naturally. Even so, they

are treated thoroughly here, unlike in other texts that deal with them only superficially. For the curious, helpful syntax and function quick references can be found in the appendices.

The following list contains other highlights of *Essential MATLAB for Engineers and Scientists, Sixth Edition*:

- Warnings of the many pitfalls that await the unwary beginner
- Numerous examples taken from science and engineering (simulation, population modeling, numerical methods) as well as business and everyday life
- An emphasis on programming style to produce clear, readable code
- Comprehensive chapter summaries
- Chapter exercises (answers and solutions to many of which are given in an appendix)
- A thorough, instructive index

Essential MATLAB is meant to be used in conjunction with the MATLAB software. The reader is expected to have the software at hand in order to work through the exercises and thus discover how MATLAB does what it is commanded to do. Learning any tool is possible only through hands-on experience. This is particularly true with computing tools, which produce correct answers only when the commands they are given and the accompanying data input are correct and accurate.

ACKNOWLEDGMENTS

I would like to thank Mary, Clara, Zoe Rae and Zach T. for their support and encouragement. I dedicate the sixth edition of *Essential MATLAB for Engineers and Scientists* to them.

Daniel T. Valentine

1

PART

Essentials

Part 1 concerns those aspects of MATLAB that you need to know in order to come to grips with MATLAB's essentials and those of technical computing. Because this book is a tutorial, you are encouraged to use MATLAB extensively while you go through the text.

Introduction

THE OBJECTIVES OF THIS CHAPTER ARE:

- To enable you to use some simple MATLAB commands from the Command Window.
- To examine various MATLAB desktop and editing features.
- To learn some of the new features of the MATLAB R2016a Desktop.
- To learn to write scripts in the Editor and Run them from the Editor.
- To learn some of the new features associated with the tabs (in particular, the PUBLISH and APPS features).

MATLAB is a powerful technical computing system for handling scientific and engineering calculations. The name MATLAB stands for Matrix Laboratory, because the system was designed to make matrix computations particularly easy. A matrix is an array of numbers organized in m rows and n columns. An example is the following $m \times n = 2 \times 3$ array:

$$A = \begin{pmatrix} 1 & 3 & 5 \\ 2 & 4 & 6 \end{pmatrix}$$

Any one of the elements in a matrix can be plucked out by using the row and column indices that identify its location. The elements in this example are plucked out as follows: $A(1, 1) = 1$, $A(1, 2) = 3$, $A(1, 3) = 5$, $A(2, 1) = 2$, $A(2, 2) = 4$, $A(2, 3) = 6$. The first index identifies the row number counted from top to bottom; the second index is the column number counted from left to right. This is the convention used in MATLAB to locate information in an array. A computer is useful because it can do numerous computations quickly, so operating on large numerical data sets listed in tables as arrays or matrices of rows and columns is quite efficient.

This book assumes that you have never used a computer before to do the sort of scientific calculations that MATLAB handles, but are able to find your way

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Summary	30	around a computer keyboard and know your operating system (e.g., Windows, UNIX or MAC-OS). The only other computer-related skill you will need is some very basic text editing.
Exercises	31	
Supplementary material	31	One of the many things you will like about MATLAB (and that distinguishes it from many other computer programming systems, such as C++ and Java) is that you can use it <i>interactively</i> . This means you type some commands at the special MATLAB prompt and get results immediately. The problems solved in this way can be very simple, like finding a square root, or very complicated, like finding the solution to a system of differential equations. For many technical problems, you enter only one or two commands—MATLAB does most of the work for you.

There are three essential requirements for successful MATLAB applications:

- You must learn the *exact* rules for writing MATLAB statements and using MATLAB utilities.
- You must know the mathematics associated with the problem you want to solve.
- You must develop a logical plan of attack—the algorithm—for solving a particular problem.

This chapter is devoted mainly to the first requirement: learning some basic MATLAB rules. Computer programming is a precise science (some would also say an art); you have to enter statements in *precisely* the right way. There is a saying among computer programmers: *Garbage in, garbage out*. It means that if you give MATLAB a garbage instruction, you will get a garbage result.

With experience, you will be able to design, develop and implement computational and graphical tools to do relatively complex science and engineering problems. You will be able to adjust the look of MATLAB, modify the way you interact with it, and develop a toolbox of your own that helps you solve problems of interest. In other words, you can, with significant experience, customize your MATLAB working environment.

As you learn the basics of MATLAB and, for that matter, any other computer tool, remember that applications do nothing randomly. Therefore, as you use MATLAB, observe and study all responses from the command-line operations that you implement, to learn what this tool does and does not do. To begin an investigation into the capabilities of MATLAB, we will do relatively simple problems that we know the answers because we are evaluating the tool and its capabilities. This is always the first step. As you learn about MATLAB, you are also going to learn about programming, (1) to create your own computational tools, and (2) to appreciate the difficulties involved in the design of efficient, robust and accurate computational and graphical tools (i.e., computer programs).

In the rest of this chapter we will look at some simple examples. Don't be concerned about understanding exactly what is happening. Understanding will come with the work you need to do in later chapters. It is very important for you to practice with MATLAB to learn how it works. Once you have grasped the basic rules in this chapter, you will be prepared to master many of those presented in the next chapter and in the Help files provided with MATLAB. This will help you go on to solve more interesting and substantial problems. In the last section of this chapter you will take a quick tour of the MATLAB desktop.

1.1 USING MATLAB

Either MATLAB must be installed on your computer or you must have access to a network where it is available. Throughout this book the latest version at the time of writing is assumed (Version R2016a).

To start from Windows, double-click the MATLAB icon on your Windows desktop. To start from UNIX, type `matlab` at the operating system prompt. To start from MAC-OS open X11 (i.e., open an X-terminal window), then type `matlab` at the prompt. The MATLAB desktop opens as shown in [Figure 1.1](#). The window in the desktop that concerns us for now is the Command Window, where the special `>>` prompt appears. This prompt means that MATLAB is waiting for a command. You can quit at any time with one of the following ways:

- Click the X (close box) in the upper right-hand corner of the MATLAB desktop.
- Type `quit` or `exit` at the Command Window prompt followed by pressing the 'enter' key.

Starting MATLAB automatically creates a folder named MATLAB in the user's Documents Folder. This feature is quite convenient because it is the default working folder. It is in this folder that anything saved from the Command Window will be saved. Now you can experiment with MATLAB in the Command Window. If necessary, make the Command Window active by placing the cursor in the Command Window and left-clicking the mouse button anywhere inside its border.

1.1.1 Arithmetic

Since we have experience doing arithmetic, we want to examine if MATLAB does it correctly. This is a required step to gain confidence in any tool and in our ability to use it.

Type `2+3` after the `>>` prompt, followed by **Enter** (press the **Enter** key) as indicated by `<Enter>`:

```
>> 2+3 <Enter>
```

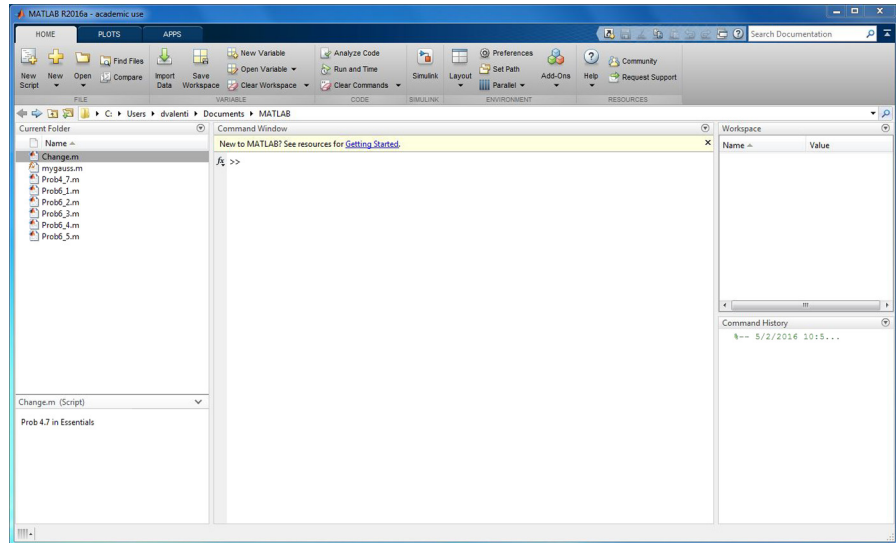


FIGURE 1.1 MATLAB desktop illustrating the Home task bar (version 2016a).

Commands are only carried out when you enter them. The answer in this case is, of course, 5. Next try

```
>> 3-2 <Enter>
>> 2*3 <Enter>
>> 1/2 <Enter>
>> 2^3 <Enter>
>> 2\11 <Enter>
```

What about $(1)/(2)$ and $(2)^(3)$? Can you figure out what the symbols $*$, $/$, and $^$ mean? Yes, they are multiplication, division and exponentiation. The backslash means the denominator is to the left of the symbol and the numerator is to the right; the result for the last command is 5.5. This operation is equivalent to $11/2$.

Now enter the following commands:

```
>> 2 .* 3 <Enter>
>> 1 ./ 2 <Enter>
>> 2 .^ 3 <Enter>
```

A period in front of the $*$, $/$, and $^$, respectively, does not change the results because the multiplication, division, and exponentiation is done with single numbers. (An explanation for the need for these symbols is provided later when we deal with arrays of numbers.)

Here are hints on creating and editing command lines:

- The line with the `>>` prompt is called the *command line*.
- You can edit a MATLAB command before pressing **Enter** by using various combinations of the **Backspace**, **Left-arrow**, **Right-arrow**, and **Del** keys. This helpful feature is called *command-line editing*.
- You can select (and edit) commands you have entered using **Up-arrow** and **Down-arrow**. Remember to press **Enter** to have the command carried out (i.e., to *run* or to *execute* the command).
- MATLAB has a useful editing feature called *smart recall*. Just type the first few characters of the command you want to recall. For example, type the characters `2*` and press the **Up-arrow** key—this recalls the most recent command starting with `2*`.

How do you think MATLAB would handle $0/1$ and $1/0$? Try it. If you insist on using ∞ in a calculation, which you may legitimately wish to do, type the symbol `Inf` (short for *infinity*). Try `13+Inf` and `29/Inf`.

Another special value that you may meet is `NaN`, which stands for *Not-a-Number*. It is the answer to calculations like $0/0$.

1.1.2 Variables

Now we will assign values to variables to do arithmetic operations with the variables. First enter the command (*statement* in programming jargon) `a = 2`. The MATLAB command line should look like this:

```
>> a = 2 <Enter>
```

The `a` is a *variable*. This statement *assigns* the value of 2 to it. (Note that this value is displayed immediately after the statement is executed.) Now try entering the statement `a = a + 7` followed on a new line by `a = a * 10`. Do you agree with the final value of `a`? Do we agree that it is 90?

Now enter the statement

```
>> b = 3; <Enter>
```

The semicolon (`;`) prevents the value of `b` from being displayed. However, `b` still has the value 3, as you can see by entering without a semicolon:

```
>> b <Enter>
```

Assign any values you like to two variables `x` and `y`. Now see if you can assign the *sum* of `x` and `y` to a third variable `z` in a single statement. One way of doing this is

```
>> x = 2; y = 3; <Enter>
>> z = x + y <Enter>
```

Notice that, in addition to doing the arithmetic with variables with assigned values, several commands separated by semicolons (or commas) can be put on one line.

1.1.3 Mathematical functions

MATLAB has all of the usual mathematical functions found on a scientific-electronic calculator, like `sin`, `cos`, and `log` (meaning the *natural* logarithm). See Appendix B.5 for many more examples.

- Find $\sqrt{\pi}$ with the command `sqrt(pi)`. The answer should be 1.7725. Note that MATLAB knows the value of `pi` because it is one of its many built-in functions.
- Trigonometric functions like `sin(x)` expect the argument `x` to be in *radians*. Multiply degrees by $\pi/180$ to get radians. For example, use MATLAB to calculate `sin(90°)`. The answer should be 1 (`sin(90*pi/180)`).
- The exponential function e^x is computed in MATLAB as `exp(x)`. Use this information to find e and $1/e$ (2.7183 and 0.3679).

Because of the numerous built-in functions like `pi` or `sin`, care must be taken in the naming of user-defined variables. Names should not duplicate those of built-in functions without good reason. This problem can be illustrated as follows:

```
>> pi = 4 <Enter>
>> sqrt(pi) <Enter>
>> whos <Enter>
>> clear pi <Enter>
>> whos <Enter>
>> sqrt(pi) <Enter>
>> clear <Enter>
>> whos <Enter>
```

Note that `clear` executed by itself clears all local variables in the *workspace*; `>>clear pi` clears the locally defined variable `pi`. In other words, if you decide to redefine a built-in function or command, the new value is used! The command `whos` is executed to determine the list of local variables or commands presently in the workspace. The first execution of the command `pi = 4` in the above example displays your redefinition of the built-in `pi`: a 1-by-1 (or 1x1) *double array*, which means this *data type* was created when `pi` was assigned a number (you will learn more about other data types later, as we proceed in our investigation of MATLAB).

1.1.4 Functions and commands

MATLAB has numerous general functions. Try `date` and `calendar` for starters. It also has numerous *commands*, such as `clc` (for *clear command window*). `help` is one you will use a lot (see below). The difference between functions and

commands is that functions usually return with a value (e.g., the date), while commands tend to change the environment in some way (e.g., clearing the screen or saving some statements to the workspace).

1.1.5 Vectors

Variables such as a and b that were used in Section 1.1.2 above are called *scalars*; they are single-valued. MATLAB also handles *vectors* (generally referred to as *arrays*), which are the key to many of its powerful features. The easiest way of defining a vector where the elements (components) increase by the same amount is with a statement like

```
>> x = 0 : 10; <Enter>
```

That is a *colon* (`:`) between the 0 and the 10. There is no need to leave a space on either side of it, except to make it more readable. Enter x to check that x is a vector; it is a *row vector*—consisting of 1 row and 11 columns. Type the following command to verify that this is the case:

```
>> size(x) <Enter>
```

Part of the real power of MATLAB is illustrated by the fact that other vectors can now be defined (or created) in terms of the just defined vector x . Try

```
>> y = 2 .* x <Enter>
>> w = y ./ x <Enter>
```

and

```
>> y = sin(x) <Enter>
```

(no semicolons). Note that the first command line creates a vector y by multiplying each element of x by the factor 2. The second command line is an array operation, creating a vector w by taking each element of y and dividing it by the corresponding element of x . Since each element of y is two times the corresponding element of x , the vector w is a row vector of 11 elements all equal to 2. Finally, z is a vector with $\sin(x)$ as its elements.

To draw a reasonably nice graph of $\sin(x)$, simply enter the following commands:

```
>> x = 0 : 0.1 : 10; <Enter>
>> z = sin(x); <Enter>
>> plot(x,z), grid <Enter>
```

The graph appears in a separate figure window. To draw the graph of the sine function illustrated in [Figure 1.2](#) replace the last line above with

```
>> plot(x,y,'-rs','LineWidth',2,'MarkerEdgeColor','k','MarkerSize',5),grid
<Enter>
```

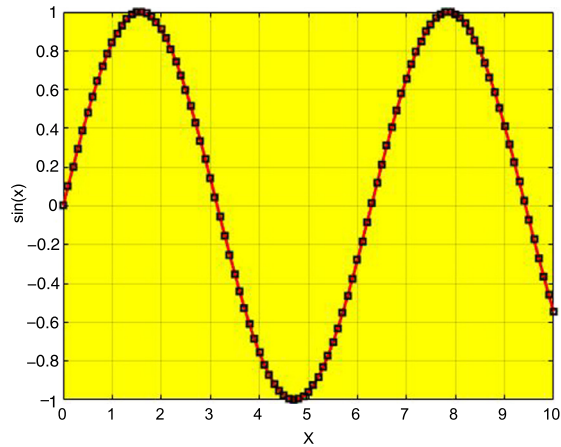


FIGURE 1.2 Figure window.

```
>> xlabel(' x '), ylabel(' sin(x) ') <Enter>
>> whitebg('y') <Enter>
```

You can select the Command Window or figure windows by clicking anywhere inside them. The **Windows** pull-down menus can be used in any of them.

Note that the first command line above has three numbers after the equal sign. When three numbers are separated by two colons in this way, the middle number is the *increment*. The increment of 0.1 was selected to give a reasonably smooth graph. The command `grid` following the comma in the last command line adds a grid to the graph.

Modifying the plot function as illustrated above, of the many options available within this function, four were selected. A comma was added after the variable `y` followed by `'rs'`. This selects a solid red line (`-r`) to connect the points at which the sine is computed; they are surrounded by square (`s`) markers in the figure. The line width is increased to 2 and the marker edge color is black (`k`) with size 5. Axis labels and the background color were changed with the statements following the plot command. (Additional changes in background color, object colors etc. can be made with the figure properties editor; it can be found in the pull-down menu under **Edit** in the figure toolbar. Many of the colors in the figures in this book were modified with the figure-editing tools.)

If you want to see more cycles of the sine graph, use command-line editing to change `sin(x)` to `sin(2*x)`.

Try drawing the graph of `tan(x)` over the same domain. You may find aspects of your graph surprising. To help examine this function you can improve the graph by using the command `axis([0 10 -10 10])` as follows:


```
>> x = 1:0.1:10; <Enter>
>> z = tan(x); <Enter>
>> plot(x,z),axis([0 10 -10 10]) <Enter>
```

An alternative way to examine mathematical functions graphically is to use the following command:

```
>> ezplot('tan(x)') <Enter>
```

The apostrophes around the function `tan(x)` are important in the `ezplot` command. Note that the default domain of `x` in `ezplot` is *not* 0 to 10.

A useful Command Window editing feature is *tab completion*: Type the first few letters of a MATLAB name and then press **Tab**. If the name is unique, it is automatically completed. If it is not unique, press **Tab** a second time to see all the possibilities. Try by typing `ta` at the command line followed by **Tab** twice.

1.1.6 Linear equations

Systems of linear equations are very important in engineering and scientific analysis. A simple example is finding the solution to two simultaneous equations:

$$x + 2y = 4$$

$$2x - y = 3$$

Here are two approaches to the solution.

Matrix method. Type the following commands (exactly as they are):

```
>> a = [1 2; 2 -1]; <Enter >
>> b = [4; 3]; <Enter >
>> x = a\b <Enter >
```

The result is

```
x =
     2
     1
```

i.e., $x = 2$, $y = 1$.

Built-in solve function. Type the following commands (exactly as they are):

```
>> [x,y] = solve('x+2*y=4','2*x - y=3') <Enter >
>> whos <Enter >
>> x = double(x), y=double(y) <Enter >
>> whos <Enter >
```

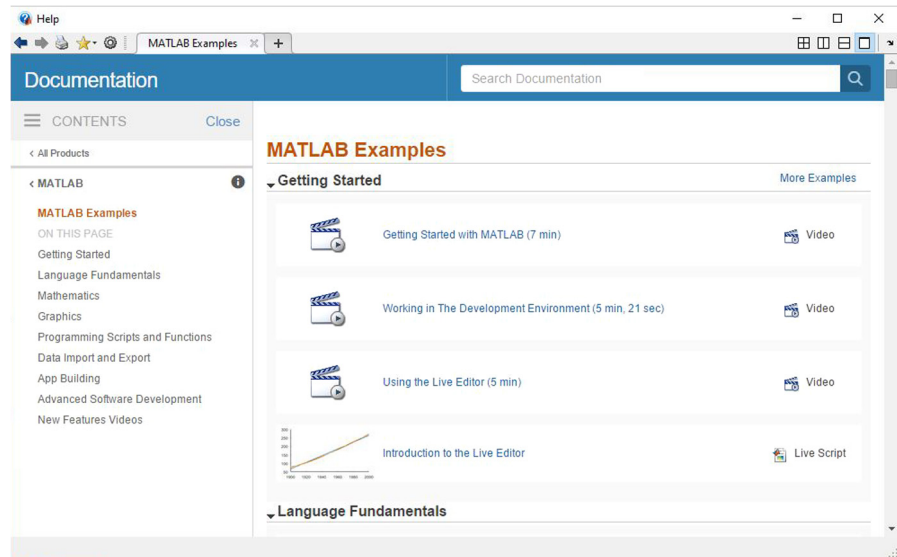


FIGURE 1.3 The Help documentation on MATLAB Examples.

The function *double* converts x and y from symbolic objects (another *data type* in MATLAB) to double arrays (i.e., the numerical-variable data type associated with an assigned number).

To check your results, after executing either approach, type the following commands (exactly as they are):

```
>> x + 2*y % should give ans = 4 <Enter>
>> 2*x - y % should give ans = 3 <Enter>
```

The % symbol is a *flag* that indicates all information to the right is *not* part of the command but a comment. (We will examine the need for comments when we learn to develop coded programs of command lines later on.)

1.1.7 Tutorials and demos

If you want a spectacular sample of what MATLAB has to offer, type the command `demo` on the command line. After entering this command the Help documentation is opened at MATLAB Examples (see Figure 1.3). Left-click on “Getting Started”. This points you to the list of tutorials and demonstrations of MATLAB applications that are at your disposal. Click on any of the other topics to learn more about the wealth of capabilities of MATLAB. You may wish to review the tutorials appropriate to the topics you are examining as part of your technical computing needs. Scroll down to the “New Features Video” to learn more about the Desktop and other new features, some of which are introduced next.

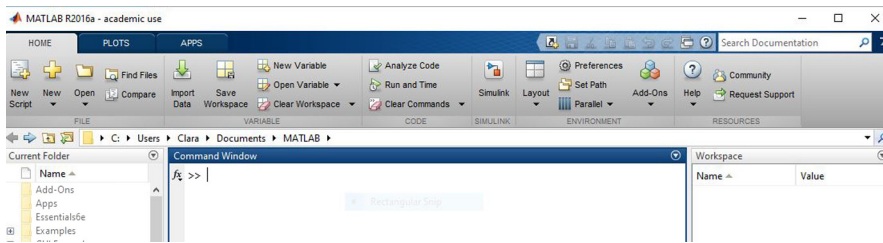


FIGURE 1.4 New Desktop Toolbar on MATLAB 2016a.

1.2 THE DESKTOP

A very useful feature of MATLAB R2016a is the fact that when you first open it, it creates the folder named MATLAB (if it does not already exist) in your Documents folder. The first time it does this, there are no items in the folder and, hence, the Current Folder panel will be empty. This new folder in your Documents is the default working folder where all the files your create are saved. The location of this folder is given in the first toolbar above the Command Window. The location is `C:\Users\Clara\Documents\MATLAB`. This format of the location was determined by pointing and left-clicking the mouse in the line just above the Command Window.

Let us examine the Desktop from the top down. On the left side of the top line you should see the name of the version of MATLAB running. In this case it is MATLAB R2016a. On the right side of the top line are three buttons. They are the underscore button, which allows you to minimize the size of the Desktop window, the rectangle button, which allows you to maximize the size of the Desktop, and the \times button, which allows you to close MATLAB (see [Figure 1.4](#)).

On the next line of the Desktop there are three tabs on the left side. The first tap is most forward in the figure and, hence, the Home toolbar is displayed (the tabs and the toolbars associated with the tabs are the main new features of this release of MATLAB). If you are already familiar with a previous release of MATLAB, you will find that these new features enhance significantly the use of MATLAB. In addition, all previously developed tools operate exactly as they did in previous releases of MATLAB. The other two tabs are PLOTS and APPS. These features allow you to access tools within MATLAB by pointing and clicking and, hence, enhance the utilization of tools and toolboxes available within MATLAB. In addition, the APPS environment allows the user to create their own applications (or APPS).

1.2.1 Using the Editor and running a script

Point and click on the New Script icon on the left most side of the Home toolbar. Doing this opens the editor in the center of the Desktop as shown in

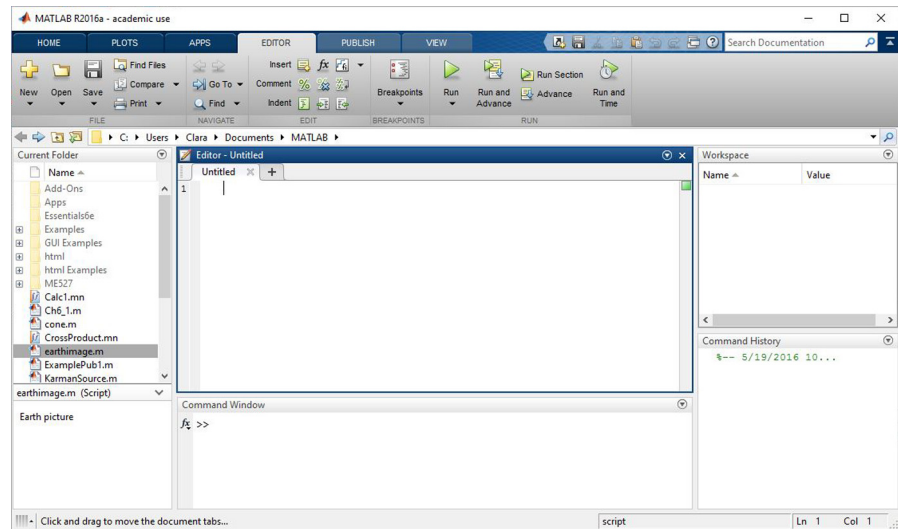


FIGURE 1.5 Editor opened in default location; it is in the center of the Desktop.

Figure 1.5. Note that three new tabs appear and that the tab that is visible is the Editor tab that is connected with the Editor. The other two tabs are Publish and View. The latter are useful when creating notebooks or other documents connected with your technical computing work. The application of these tools will be illustrated by an example later in this text.

Let us first consider using the Editor. Type into the Editor the following script:

```
% Example of one of the matrix inversion methods available in MATLAB
clear;clc
% Let us consider the following arbitrarily selected matrix:
A =magic(3)
% Let us evaluate its inverse as follows:
AI = inv(A)
% Let us check that it is an inverse:
IPredicted = A * AI
% This is the exact unitary matrix:
IM = eye(3)
% This is the difference between the exact and predict unitary
% matrix:
difference = IPredicted - IM
for m = 1:3
    for n = 1:3
        if difference(m,n) < eps;
            IPredicted(m,n) = IM(m,n);
        end
    end
end
end
```

```
IPredicted
IPredicted == IM
```

Then click on the Run button just under the tab named View. The first time the script is executed you are asked to name the file. The name used in this example is `ExA1_1.m`. If all lines are typed correctly (except the lines beginning with the symbol `'%'`, because they are comments that have nothing to do with the sequence of commands in the script except that they help the reader understand what the script does), what shows up in the Command Window is as follows:

```
A =
     8     1     6
     3     5     7
     4     9     2

AI =
    0.1472   -0.1444    0.0639
   -0.0611    0.0222    0.1056
   -0.0194    0.1889   -0.1028

IPredicted =
    1.0000         0   -0.0000
   -0.0000    1.0000         0
    0.0000         0    1.0000

IM =
     1     0     0
     0     1     0
     0     0     1

difference =
    1.0e-15 *
         0         0   -0.1110
   -0.0278         0         0
    0.0694         0         0

IPredicted =
     1     0     0
     0     1     0
     0     0     1

ans =
     1     1     1
     1     1     1
     1     1     1
```

The `IPredicted` matrix is supposed to be the identity matrix, `IM`. The matrix `IPredicted` was determined by multiplying the matrix `A` by its numerically computed inverse, `AI`. The last print out of `IPredicted` is a modification of the original matrix; it was changed to the elements of the `IM` matrix if the difference between a predicted and an actual element of `IM` was less than

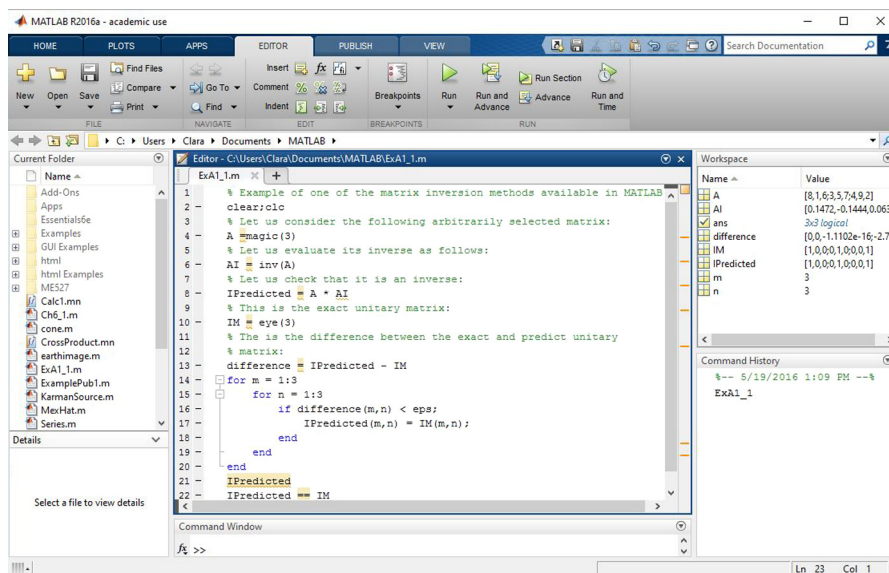


FIGURE 1.6 Sample script created and executed in the first example of this section.

$\text{eps} = 2.2204e - 16$. Since the result is identical to the identity matrix, this shows that the inverse was computed correctly (at least to within the computational error of the computing environment, i.e., $0 < \text{eps}$). This conclusion is a result of the fact that the `ans` in the above example produced the logical result of 1 (or `true`) for all entries in the adjusted `IPredicted` matrix as logically compared with the corresponding entries in `IM`.

At this point in the exercise the Desktop looks like Figure 1.6. The name of the file is `ExA1_1.m`. It appears in the Current Folder and it also appears in the Command History. Note that the Workspace is populated with the variables created by this script.

This concludes the introduction of the most important tools needed for most of the exercises in Essential MATLAB (i.e., in this text). In the next section we examine an example of some of the other new features of MATLAB R2016a.

1.2.2 Help, publish and view

Publish is an easy way to create notebooks or other documents in `html` format. The conversion of the information typed into an M-file is published into a document that looks like the new `Help` environment. To open the help documents go to the top of the Desktop to the question mark. Left click on the question mark `?`. The Help window opens up. Left click on the topic "MATLAB" to open up the window illustrated in Figure 1.7. This also illustrates the new format

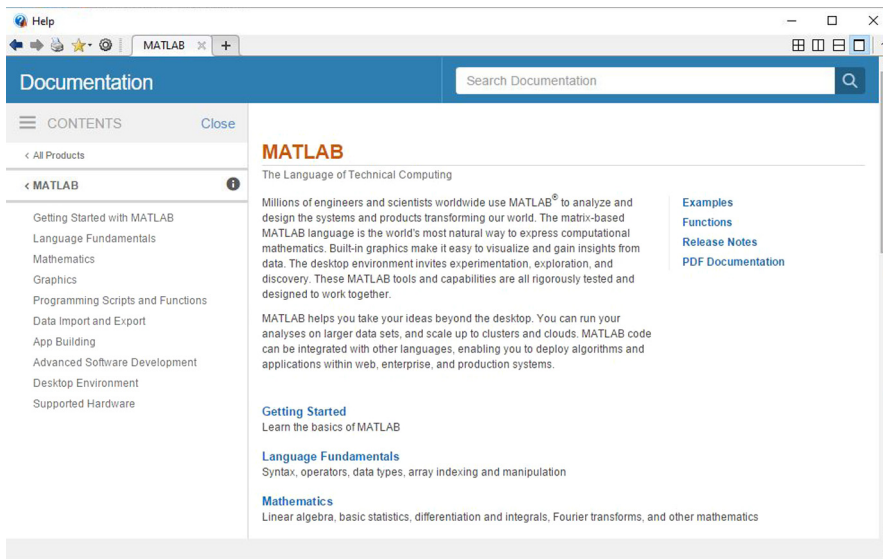


FIGURE 1.7 Illustration of one of the pages in the online documentation for MATLAB.

of the searchable documentation available within MATLAB R2016a. We want to compare this documentation with the kind you can PUBLISH yourself. To illustrate how easy it is to create documents like the MATLAB documents, let us consider the following simple example.

Click the New Script button to open up the editor (or type `edit` after the command prompt in the Command Window followed by tapping the enter key). The Editor tab is in the most forward position on the main taskbar. Place the cursor on PUBLISH and left click on the mouse. This brings the PUBLISH toolbar forward. Left click Section with Title. Replace SECTION TITLE with PUBLISHING example. Next, replace DESCRIPTIVE TEXT with

```
%%
% This is an example to illustrate how easy it is to create a document
% in the PUBLISH environment.
%
% (1) This is an illustration of a formula created with a LaTeX command:
%
```

Next, click on Σ Inline LaTeX located in the “Insert Inline Markup” group. This leads to the addition of the equation $x^2 + e^{-\pi i}$. Following this equation add the text shown in the final script file shown below that ends with “clicked:”. This is followed by a blank line and a command script; this command script is included to illustrate how MATLAB commands can be incorporated into published documents.

```

%%
% This is an example to illustrate how easy it is to create a document
% in the PUBLISH environment.
%
% (1) This is an illustration of a formula created with a LaTeX command:
%
%%
%  $x^2+e^{\pi i}$ 
%
% (2) This is an illustration of how you can incorporate a MATLAB script
% in the document that is run when the Publish button below and to the
% right of View is clicked:

% Earth picture
load earth
image(X); colormap(map);
axis image

```

The final step is to left-click on Publish, which is just to the right and below View. The first window to appear is the one asking you to save the M-file. The name used in this example is `ExamplePub1.m`. After it appears in the Current Folder it is executed. A folder named `html` is automatically created and it contains the html document just created. The document is illustrated in [Figure 1.8](#).

Finally, the VIEW tab brings up a toolbar that allows you to change the configuration of the Editor window. From the authors point of view, the default Editor environment is fine as is especially for users who are beginning to use MATLAB for technical computing. Customizing your working environment is certainly possible in MATLAB. However, it is useful to learn how to deal with the default environment before deciding what needs to be changed to help satisfy your own requirements for using MATLAB.

1.2.3 Symbolics and the MuPAD notebook APP

The Symbolic Math Toolbox is a useful tool to help you do symbolic mathematical analysis. It has been made much more accessible through the application called the MuPAD Notebook APP. To open this APP start by a left-click on the APPS tab in the second line from the top on the desktop shown in [Figure 1.4](#). This operation brings the APPS toolbar forward as illustrated in [Figure 1.9](#). Left-click on the MuPAD Notebook APP. The window in [Figure 1.10](#) is the notebook environment that opens up. The left bracket on the upper left side of the white note pad is where the commands are typed. The panel on the right side of the pad is the Command Bar. It provides easy access to many of the commands needed to do mathematics including the manipulation and evaluation of mathematical expressions as well as plotting graphs. The two toolbars above the pad provide useful utilities to enhance your usage of MuPAD. Moving the cursor over the items on the second line tells you what each button

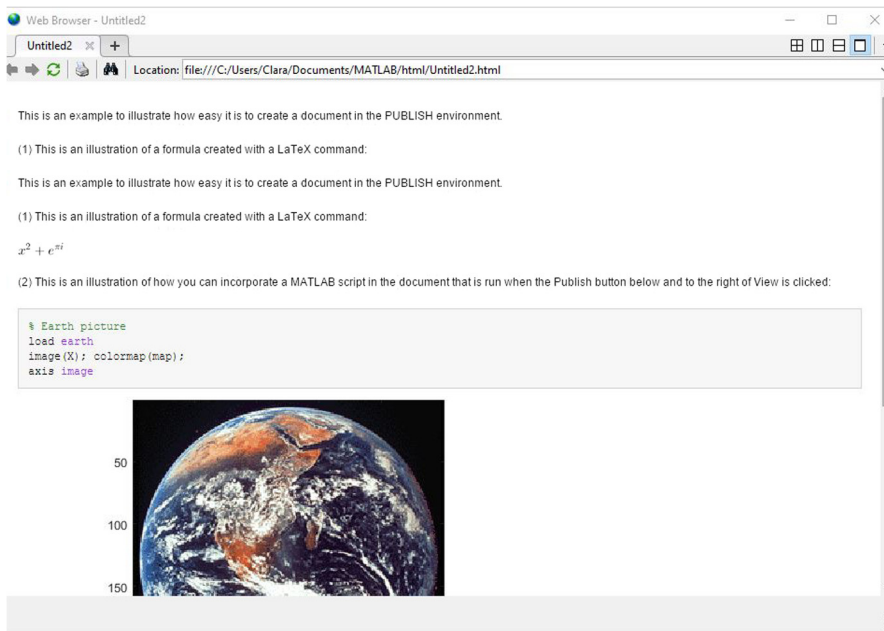


FIGURE 1.8 Sample document created in the Publish environment.

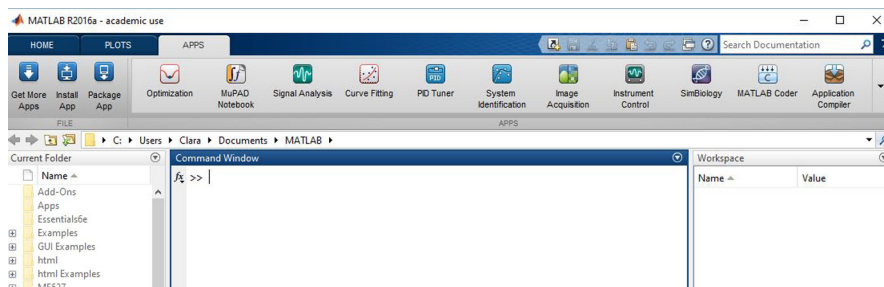


FIGURE 1.9 The APPS toolbar on the Desktop.

does. The first line requires moving the cursor over them and a left-click on the mouse to open the pull-down menu. This toolbar is common to all windows of the MATLAB technical computing environment. Let us examine a simple example.

Left-click in the note pad just above the left bracket. At this location you can start typing text (i.e., your notes on the mathematical work you are about to begin in this notebook). [Figure 1.11](#) illustrates a simple example of taking the derivative of a function and then integrating the result to learn more about the relationship between differentiation and integration in the calculus. This note-

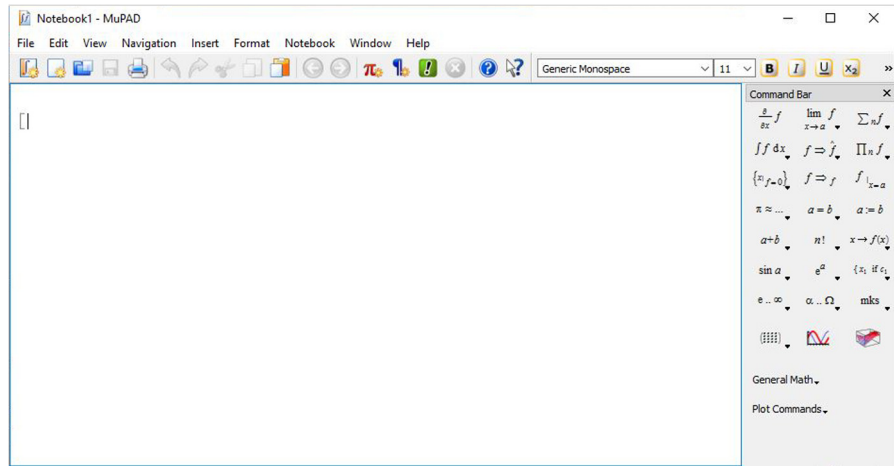


FIGURE 1.10 The MuPAD window or notebook.

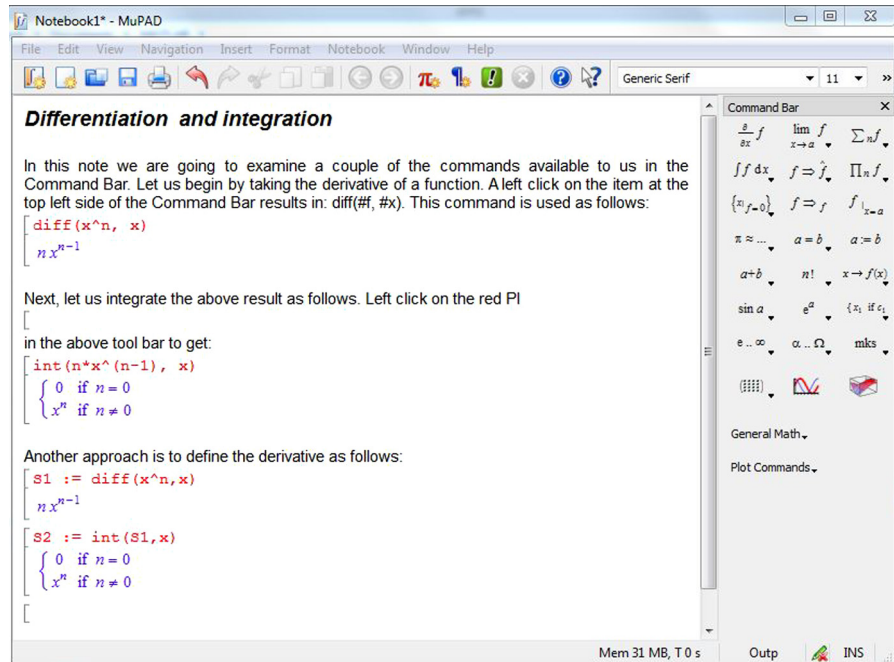


FIGURE 1.11 The MuPAD notebook Calc1.mn.

book was saved under the name `Calc1.mn`. Note the file extension (`*.mn`) for MATLAB notebooks created in MuPAD. Double-left clicking on the file with this filename in the Command Folder panel opens this notebook (as it is illus-

trated in the figure). The details of this example are also provided in the figure. They are as follows:

Differentiation and integration

In this note we are going to examine a few of the mathematical commands available to us and listed in the Command Bar. Let us begin with taking the derivative of a function f . With the cursor placed on the upper left most symbol, a left-click on the mouse produces the following result: `diff(#f, #x)`. The $\#$ sign is a place holder at which input is required. The next step is to point to the right of the left bracket below and left-click to place the note pad cursor at this location. Then click on the command of interest in the Command Bar. Change $\#f$ to x^n and $\#x$ to x . Then hit enter to execute the command. The result is:

```
[diff(x^n, x)
n x^{n-1}
```

Next, let us integrate this result. First let us save the result under the name $S1$ as follows:

```
[S1 := diff(x^n, x)
n x^{n-1}
```

Now, let us integrate. Left-click on this operation in the Command Bar to get: `int(#f, #x)`. Replace $\#f$ with $S1$ and $\#x$ with x . Thus,

```
[S2 := int(S1, x)
{ 0   if n = 0
{ x^n if n ≠ 0
```

Hence, integration is, as expected, the inverse of differentiation. The only issue, if any, that you must keep in mind is that the constants of integration are set to zero. If you need to explicitly carry them along in your analysis, then you must add a constant to the results at this step.

REMARK: Help is available through the help documentation. The help can be accessed by a left click on the blue circle with the question mark in the toolbar just above this pad.

A second example is the graphics capabilities in MuPAD. There are other plotting utilities within MATLAB that allow you to examine functions graphically and quickly. The MuPAD environment is particularly well suited for this kind of investigation. Suppose you are reading a technical article and you come across two interesting functions and you want to have an idea as to what they look like. Let us examine two examples. One is the $\text{sech}^2(x)$ function which plays an important role in nonlinear wave theory. The second is the complete

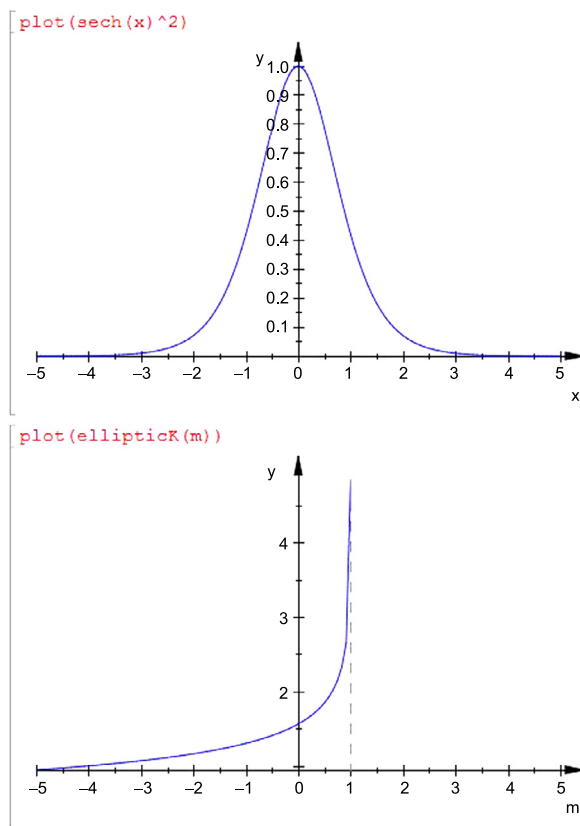


FIGURE 1.12 Illustration of MuPAD graphics.

elliptic integral of the first kind, viz.,

$$K(m) = \int_0^{\pi/2} \frac{1}{\sqrt{1 - m^2 \sin^2 \theta}} d\theta$$

This integral plays an important role in potential theory. What do these functions look like? The MuPAD notebook in [Figure 1.12](#) illustrates the shapes of these functions. More on these functions among other functions can be examined in the help documentation and in the references cited in the help documentation.

This concludes this brief introduction to an APP and a brief introduction to the capabilities of the Symbolic Math toolbox.

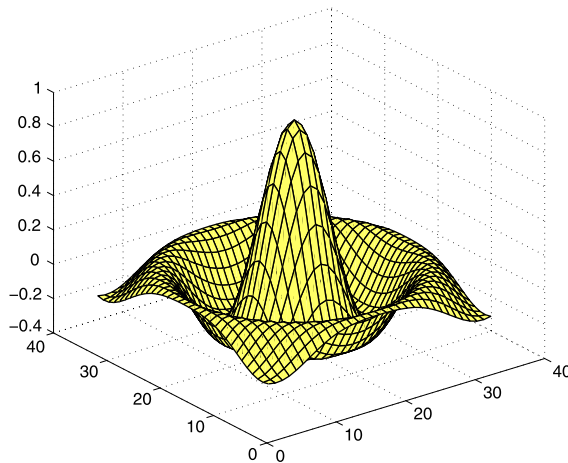


FIGURE 1.13 The Mexican hat.

1.2.4 Other APPS

There are a number of other APPS available from MathWorks. In addition, there is a capability for you to create your own APPS. Hence, if there is anything that we learn from our first experiences with MATLAB is that there is a lot to learn (a lifelong experience of learning) because of the wealth of technology incorporated in this technical computing environment. The fact that you can develop your own toolboxes, your own APPS and you can customize your working environment (desktop arrangement, color backgrounds, fonts, graphical user interfaces and so on) provides real opportunities and useful experience in creating designs, creating useful tools and documenting your work.

1.2.5 Additional features

MATLAB has other good things. For example, you can generate a 10-by-10 (or 10×10) *magic square* by executing the command `magic(10)`, where the rows, columns, and main diagonal add up to the same value. Try it. In general, an $n \times n$ magic square has a row and column sum of $n(n^2 + 1)/2$.

You can even get a *contour* plot of the elements of a magic square. MATLAB pretends that the elements in the square are heights above sea level of points on a map, and draws the contour lines. `contour(magic(32))` looks interesting.

If you want to see the famous Mexican hat (Figure 1.13), enter the following four lines (be careful not to make any typing errors):

```
>> [x y ] = meshgrid(-8 : 0.5 : 8); <Enter>
>> r = sqrt(x.^2 + y.^2) + eps; <Enter>
>> z = sin(r) ./ r; <Enter>
```

```
>> mesh(z); <Enter>
```

`surf(z)` generates a faceted (tiled) view of the surface. `surfc(z)` or `meshc(z)` draws a 2D contour plot under the surface. The command

```
>> surf(z), shading flat <Enter>
```

produces a nice picture by removing the grid lines.

The following animation is an extension of the Mexican hat graphic in [Figure 1.13](#). It uses a `for` loop that repeats the calculation from $n = -3$ to $n = 3$ in increments of 0.05. It begins with a `for n = -3:0.05:3` command and ends with an `end` command and is one of the most important constructs in programming. The execution of the commands between the `for` and `end` statements repeat 121 times in this example. The `pause(0.05)` puts a time delay of 0.05 seconds in the `for` loop to slow the animation down, so the picture changes every 0.05 seconds until the end of the computation.

```
>> [x y]=meshgrid(-8:0.5:8); <Enter>
>> r=sqrt(x.^2+y.^2)+eps; <Enter>
>> for n=-3:0.05:3; <Enter>
>> z=sin(r.*n)./r; <Enter>
>> surf(z), view(-37, 38), axis([0,40,0,40,-4,4]); <Enter>
>> pause(0.05) <Enter>
>> end <Enter>
```

You can examine sound with MATLAB in any number of ways. One way is to listen to the signal. If your PC has a speaker, try

```
>> load handel <Enter>
>> sound(y,Fs) <Enter>
```

for a snatch of Handel's Hallelujah Chorus. For different sounds try loading `chirp`, `gong`, `laughter`, `splat`, and `train`. You have to run `sound(y,Fs)` for each one.

If you want to see a view of the Earth from space, try

```
>> load earth <Enter>
>> image(X); colormap(map) <Enter>
>> axis image <Enter>
```

To enter the matrix presented at the beginning of this chapter into MATLAB, use the following command:

```
>> A = [1 3 5; 2 4 6] <Enter>
```

On the next line after the command prompt, type `A(2,3)` to pluck the number from the second row, third column.